# graphi Documentation 

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## CHAPTER 1

## Quick Usage Reference

Graph I is primarily meant for working directly on graph data. The primitives you need to familiarise yourself with are

1. graphs, which are extended containers,
2. nodes, which are arbitrary objects in a graph,
3. edges, which are connections between objects in a graph, and
4. edge values, which are values assigned to connections in a graph.


This documentation page gives an overview of the most important aspects. The complete interface of GraphI is defined and documented by Graph.

### 1.1 Creating Graphs and adding Nodes

You can create graphs empty, via cloning, from nodes or with nodes, edges and values. For many use-cases, it is simplest to start with a set of nodes:

```
from graphi import graph
planets = graph("Earth", "Jupiter", "Mars", "Pluto")
```

Once you have a graph, it works similar to a set for nodes. You can simply add() and discard() nodes:

```
planets.add("Venus")
planets.add("Mercury")
planets.discard("Pluto")
```


### 1.2 Working with Edges and Values

To really make use of a graph, you will want to add edges and give them values. Simply pick a connection from a node to a node and assign it a value:

```
# store the average distance between planets
planets["Earth":"Venus"] = 41400000
```

An edge is always of the form start:end, but values can be of arbitrary type. For example, you can easily add multiple values for a single edge using containers:

```
# add multiple values as an implicit tuple
planets["Earth":"Venus"] = 41400000, 258000000
# add multiple values as an explicit, mutable list
planets["Earth":"Mars"] = [78000000, 378000000]
```

The :-syntax of edges is not just pretty - it ensures that you never, ever accidentally mix up nodes and edges. This allows you to safely use the same graph [item] interface for nodes and edges.

If you need to define an edge outside of graph accesses, explicitly use Edge:

```
from graphi import Edge
if Edge["Venus":"Earth"] in planets:
    print("Wait, isn't there a pattern for this?")
```


### 1.3 Graphs as Python Containers

GraphI is all about letting you handle graphs with well-known interfaces. A graph is a container indexed by either nodes or edges:

```
print(planets["Venus":"Earth"])
del planets["Jupiter"]
```

Even though it contains nodes, edges and values, it presents its nodes first - similar to keys in a dict. However, you can efficiently access its various elements via views:

```
print("My father only told me about %d of our planets." % len(planets))
print("But I looked up %d distances between planets:" % len(planets.edges())
for planet_a, planet_b, distances in planets.items():
    print(" %s to %s: %s" % (planet_a, planet_b, '-'.join(distances)))
```


## CHAPTER 2

## Common Graph Operations

Many common graph operations map to simple operators in graphi. Unless parameters are needed, builtin operations usually suffice. For example, the outdegree of a node is simply its number of outgoing edges, i.e.

```
out_degree = len(graph[node])
```

in a directed graph. Since graphi makes heavy use of data views (instead of copies), this has optimal performance.

### 2.1 Pythonic Graph Operations

### 2.1.1 Nodes of a graph

Graphs behave like a set with regard to nodes. Note that removing a node also invalidates all its edges and their values.
graph[a] = True
graph.add (a)
graph.discard(a)
Safely add or remove a node a from graph.
del graph[a]
Remove a node a from graph.
a in graph
Whether there is a node a in graph.
list (graph)
iter (graph)
for a in graph:
List/iterate/traverse all nodes in graph .

## len (graph)

The number of nodes in the graph.

### 2.1.2 Edges and values of a graph

Graphs special-case edges: an edge is a secondary key, being the value to nodes and the key to edge values.

## Edge [a:b] in graph

Whether there is an edge from node a to node b in graph.

```
Loop[a] in graph
Edge[a:a] in graph
```

Whether there is a loop from node a to itself in graph.

```
list(graph[a])
iter(graph[a])
for b in graph[a]:
```

List/iterate/loop all nodes for which there is an edge from node a, i.e. its neighbours.

## len (graph[a])

The number of outgoing edges of node a, i.e. its outdegree.

### 2.1.3 Edge values of a graph

Graphs behave similar to a dict, tying values to edges. Note that removing a node also invalidates all its edges and their values.

```
graph[a:b] = w
graph[Edge[a:b]] = w
```

Add an edge from node a to node b with value w .

### 2.2 Pythonic Graph Types

By default, every graph is a weighted, directed graph - edges are oriented from start to end node and have one edge value. However, other graph types can be created with standard language features.

## graph [a:b] = True

Add an edge from node a to node b with the primitive value True.
This creates an unweighted graph edge.

```
graph[a:b] = [w1, w2, w3, ...]
graph[a:b] = w1, w2, w3, ...
```

Add an edge from node a to node b with multiple values w1, w2, w3, ....
This creates a multigraph edge.

```
graph[a:b] = graph[b:a] = w
```

Add edges from node a to node b and from node b to node a with the identical value w .
This creates an undirected graph edge.

### 2.3 Abstract Graph operations

The common abstract Graph Operations interface can be mapped to graphi almost directly. Most operations map to container accesses via [item], and an edge is represented as $x: y$.

| Graphi | Abstract Graph Operation |  |
| :---: | :---: | :---: |
| G.add (x) | add_vertex (G, x) | adds the node x |
| G.discard(x) | remove_vertex(G, x) | removes the node x |
| del G[x] | N/A | $\ldots$... but raises NodeError if there is no node x |
| G. add (Edge[x:y]) | add_edge (G, x, y) | adds an edge from node x to node y |
| G . discard (Edge [x:y] | remove_edge (G, x, y) | removes the edge from node x to node y |
| del G[x:y] | N/A | ..., but raises EdgeError if there is no edge from node $x$ to node $y$ |
| Edge[x:y] in $G$ | adjacent (G, x, y) | tests whether there is an edge from node $x$ to node $y$ |
| $\mathrm{G}[\mathrm{x}: \mathrm{y}]$ | N/A | raises EdgeError if there is no edge from node x to node y |
| list(G[x]) | neighbors (G, x) | lists all nodes y with an edge from node x to node y |
| N/A | $\begin{aligned} & \text { get_vertex_value (G, } \\ & \text { x) } \end{aligned}$ | returns the value associated with node x |
| N/A | ```set_vertex_value(G, x, v)``` | sets the value associated with node x to v |
| $\mathrm{G}[\mathrm{x}: \mathrm{y}]$ | ```get_edge_value(G, x, y)``` | returns the value associated with the edge $\mathrm{x}: \mathrm{y}$ |
| $\mathrm{G}[\mathrm{x}: \mathrm{y}]=\mathrm{w}$ | $\begin{aligned} & \text { set_edge_value (G, x, } \\ & \text { y, v) } \end{aligned}$ | sets the value associated with the edge $x: y$ to $v$ |

Note that there is no concept for associating a value to a node in a graph - for a node $\mathrm{x}, \mathrm{G}[\mathrm{x}]$ is the adjacency list. Instead, use a separate dict to assign external values to nodes, or set values directly on nodes.

Graphs use both key and slice notation to refer to nodes and edges, respectively. This works for both assignment and lookup of the respective value.

### 3.1 Nodes

A node is written directly. Its value is the adjacency associated with the node in the graph, i.e. a mapping to all neighbours and the respective edge value.

$$
\underbrace{\text { flighttime }}_{\text {graph }}[\underbrace{\text { Berlin }}_{\text {node }}]=\overbrace{\{\underbrace{\text { London }}_{\text {node }}: \underbrace{3900}_{\text {value }}, \ldots\}}^{\text {adjacency }}
$$

### 3.2 Edges

An edge is written using slice notation. Its value is the edge value associated with the edge in the graph.


## CHAPTER 4

Glossary
loop An edge from a node to itself. Counts as both an ingoing and outgoing edge for outdegree, indegree and degree. indegree The number of ingoing edges of a node. If a node has a loop, it also counts as an ingoing edge.

The number of nodes to which a node is a neighbour.
outdegree The number of outgoing edges of a node. If a node has a loop, it also counts as an outgoing edge.
The number of neighbours of a node.
degree The number of ingoing and outgoing edges of a node. If a node has a loop, it counts as both an ingoing and outgoing edge.
The degree of a node is the sum of its indegree and outdegree.
graph A collection of nodes, edges between them and possibly values associated with any edges.
node A regular object in a graph.
edge
arrow A connection between two nodes in a graph.
edge value
weight The value associated with an edge in a graph.
neighbour A node with an edge from a specific node. Given an edge $\mathrm{a}: \mathrm{b}, \mathrm{b}$ is a neighbour of a .
The number of neighbours is the outdegree.

## chapter 5

## graphi Changelog

## 5.1 prerelease 201?-??-??

Overview Added operator interface and implementations
Added graph input/output
Added Cython graph implementation
Major Changes Added graph [item] = True, which is equal to graph.add(item). Deprecates both graph[node] = node and graph[node] = None.

The class graphi.graph always uses the best implementation available
New Features Operator interface allowing graphs types to use optimized implementations
Added operators:

- neighbours(graph, node, ..)
- density(graph)

Added input formats:

- csv
- GraphML


## Minor Changes

Graphs explicitly define bool (graph). This was previously implicitly available as bool falls back to $\qquad$ len $\qquad$

### 5.2 0.2.0 2018-07-31

Notes Definition of primary interface, algorithms (Graph. neighbours) will be revised
New Features Added AdjacencyGraph

Major Changes Defined graph container interface
Minor Changes Added documentation

## chapter 6

## 6.1 graphi package

### 6.1.1 Graphl - Graphs for Humans

Documentation is available in docstrings of modules, classes and functions. In an interactive session, use help, or ipython's ? and ??. For example, use help (graphi. GraphABC) to view the graph interface.

For further help, tutorials and examples visit http://graphi.readthedocs.io to view the full documentation.

## Using Graphs

You should start by using the type graphi.graph - the most well-rounded graph implementation on your system. Like all graphi types, it uses an interface similar to the Python builtin types:

```
from graphi import graph
from datetime import timedelta
# create a graph with initial nodes
airports = graph("New York", "Rio", "Tokyo")
# add edges between nodes
airports["New York":"Rio"] = timedelta(hours=9, minutes=50)
airports["New York":"Tokyo"] = timedelta(hours=13, minutes=55)
```

All graphs behave like a blend of a set of nodes and a dict of edges. Bulk lookups, such as the adjacency of a node or edges of a graph, provide efficient views. For example, len(graph[node])' provides the number of outgoing edges from node without building intermediate containers.

```
print('There are', len(airports), 'airports in the world!')
# iterate directly on nodes...
```

```
for node in airports:
    print(node, 'has', len(airports[node]), 'outgoing connections.')
# ... or use graph.nodes(), graph.edges(), graph.values() or graph.items()
for edge in airports.edges():
    print('Origin:', edge.start, ' Destination:', edge.stop, ' Flight Time:',
\hookrightarrowairports[edge])
```

graphi.graph
alias of graphi.types.adjacency_graph.AdjacencyGraph
graphi.GraphABC
alias of graphi.abc. Graph
class graphi.Edge (start, stop, step=None)
Bases: object

An edge in a graph as a pair of nodes

## Parameters

- start - the start or tail of an edge
- stop - the stop or head of an edge
- step - currently unused

This is a verbose interface for creating edges between nodes for use in a graph. It allows using slice notation independent of a graph:

```
>>> atb = Edge[a:b]
>>> a2b = Edge(a, b)
>>> graph[a2b] = 1337
>>> graph[a:b] == graph[atb] == graph[a2b] == graph[Edge[a:b]] == graph[Edge(a,
๑b)]
True
```

A Edge can also be used for explicit containment tests:

```
>>> Edge[a:b] in graph
True
```

In addition to their slice-like nature, $E d g e$ is iterable and indexable. This allows for easy unpacking:

```
>>> edge = Edge[a:b]
>>> tail, head = edge
```

Note: This class creates a representation of an edge as a connection between nodes. Edge values can be arbitrary objects.

Warning: Even though Edge behaves like a slice in graphs, builtin containers such as list cannot make use of an Edge.

## start

stop

### 6.1.2 Subpackages

graphi.graph_io package
Subpackages
graphi.graph_io.graphml package

Utilities for loading and storing Graphs as GraphML XML

## The GraphML Format

This modules is capable of reading data according to the GraphML Specification. The GraphML format covers all functionality that can be represented by :my:mod‘graphi‘ graphs. Note that several GraphML features, such as hyperedges, are not supported.

```
<?xml version="1.0" encoding="UTF-8"?>
<graphml xmlns="http://graphml.graphdrawing.org/xmlns"
    xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance"
    xsi:schemaLocation="http://graphml.graphdrawing.org/xmlns
        http://graphml.graphdrawing.org/xmlns/1.0/graphml.xsd">
    <graph id="G" edgedefault="undirected">
        <node id="n0"/>
        <node id="n1"/>
        <node id="n2"/>
        <edge source="n0" target="n1"/>
        <edge source="n1" target="n2"/>
        <edge source="n2" target="n0"/>
    </graph>
</graphml>
```


## Submodules

## graphi.graph_io.graphml.elements module

Representations of the elements in a GraphML document

```
class graphi.graph_io.graphml.elements.DataKey(identifier, attr_name, attr_type, de-
                                    fault=None)
```

    Bases: ob ject
    A GraphML Key specification on how to convert attributes of nodes
Note Unlike the GraphML key element, no domain is stored. See KeyDomain for its equivalent.

## classmethod from_element (element)

Create a DataKey instance from a graphml key element

```
    types = {'boolean': <type 'bool'>, 'double': <type 'float'>, 'float': <type 'float'
class graphi.graph_io.graphml.elements.GraphMLEdge(identifier, source, target, directed,
                                    attributes)
    Bases: ob ject
A GraphML edge element
```

classmethod from_element (element, key_domain, default_directed)
Create a DataKey instance from a graphml edge element
class graphi.graph_io.graphml.elements.GraphMLNode (identifier, attributes)
Bases: ob ject
A GraphML node element
classmethod from_element (element, key_domain)
Create a DataKey instance from a graphml node element

```
class graphi.graph_io.graphml.elements.KeyDomain(domain, keys)
```

Bases: object
The GraphML domain to which keys apply
A KeyDomain represents all keys of a given domain. A GraphML key element with a domain is represented by a DataKey stored in the corresponding KeyDomain.

```
GRAPHML_DOMAINS = ('graph', 'node', 'edge', 'all')
```

compile_attributes (element)

Compile a dictionary of attributes from a graphml element for this domain
Note The validity of the domain is currently not checked. In the future, an error may be thrown if element is of the wrong domain.
classmethod from_graphml (domain, graphml)
Create a KeyDomain instance for a given domain from a graphml root element
class graphi.graph_io.graphml.elements.QualifiedTag (namespace, localname)
Bases: object
An XML tag consisting of (optional) namespace and local name
classmethod from_tag (tag)
Parse an \{namespace\} localname tag to a QualifiedTag

## graphi.graph_io.graphml.reader module

```
class graphi.graph_io.graphml.reader.Namespace(**kwargs)
```

Bases: ob ject
graphi.graph_io.graphml.reader.graph_reader(source, node_type=<function id_node $>, \quad$ value_type $=<$ function true_namespace_value >)
Read a graph from GraphML source

## Parameters

- source - a string, file path or file object containing GraphML data
- node_type (Callable [ GraphMLNode], Any]) - type converter for nodes
- value_type (Callable [ [GraphMLEdge], Any]) - type converter for edges

Returns Iterable[AdjacencyGraph]
Since a GraphML file may contain multiple graphs, an iterable over all contained graphs is returned.

```
# read a single graph
graph, = graph_reader(source_path)
# read several graphs
graphs = list(graph_reader(source_path))
# stream through graphs
for graph in graph_reader(source_path):
```

The node_type and value_type are used to convert the GraphML-specific GraphMLNode and GraphMLEdge to generic nodes and edge values. As edges are defined by nodes, there is no separate converter.

```
graphi.graph_io.graphml.reader.id_node(node)
```

Create nodes from their id field

```
graphi.graph_io.graphml.reader.true_namespace_value(edge)
```

All existing edges have either a True value or a Namespace if any attributes are set

## Submodules

```
graphi.graph_io.csv module
```

Utilities for loading and storing Graphs as csv

## CSV Graph Format

The CSV graph format uses an optional header to define nodes, and a body storing the adjacency matrix. By default, a graph with $n$ nodes is stored as a matrix literal of $n$ columns and $n+1$ rows:

| a | b | c | d |
| :--- | :--- | :--- | :--- |
| 0 | 2 | 1 | 0 |
| 2 | 0 | 3 | 2 |
| 1 | 4 | 0 | 0 |
| 0 | 1 | 3 | 0 |

Separators and formatting are handled by the csv Dialect. Value conversion and interpretation is handled by the appropriate reader/writer.

## Reading Graphs

Graphs can be read using graph_reader () from iterables of CSV lines, such as files or str.splitlines. The csv itself is parsed using a CSV. reader (), which allows setting the CSV dialect.

```
from graphi.graph_io import CSV
literal = """\
a, b, c
0, 2, 3
2, 0, 2
1, 2, 0
" ""
```

```
graph = csv.graph_reader(
    literal.splitlines(),
    skipinitialspace=True,
)
for nodes in graph:
    print(repr(node), "=>", graph[nodes])
```

class graphi.graph_io.csv.DistanceMatrixLiteral
Bases: csv.Dialect
CSV dialect for a Graph Matrix Literal, suitable for numeric data and string literals
A graph with alphabetic node names and numeric values would look like this:

| $a$ | $b$ | $c$ |
| ---: | ---: | ---: |
| 0 | 2 | 1.3 |
| 2 | 0 | .5 |
| 16 | .5 | 1 |

delimiter $=$ ' '
doublequote $=$ False
escapechar = '<br>'
lineterminator $=' \backslash n '$
quotechar = "'"
quoting $=0$
skipinitialspace $=$ True
exception graphi.graph_io.csv.ParserError (error, row, column=None)
Bases: exceptions.Exception
Error during parsing of a graph from a csv
graphi.graph_io.csv.graph_reader (iterable, nodes_header=True, literal_type=<function stripped_literal>, valid_edge=<type 'bool'>, undirected $=$ False, value_bound $=$ None, $* \operatorname{args}, * * k w a r g s$ )
Load a graph from files or iterables

## Parameters

- iterable - an iterable yielding lines of CSV, such as an open file
- nodes_header - whether and how to interpret a header specifying nodes
- literal_type - type callable to evaluate literals
- valid_edge - callable to test whether an edge should be inserted
- undirected - whether to mirror the underlying matrix
- value_bound - whether and how much the underlying edge values are bounded

The iterable argument can be any object that returns a line of input for each iteration step, such as a file object or a list of strings.
Nodes are created depending on the value of nodes_header:
False Nodes are numbered 1 to len (iterable[0]). Elements in the first line of iterable are not consumed by this.
iterable Nodes are read from node_header.
True Nodes are taken as the elements of the first line of iterable. The first line is consumed by this, and not considered as containing graph edges. Nodes are read plainly of type :py:class:str, not using literal_type.
callable Like True, but nodes are not taken as plain str() but individually interpreted via node_header (element).

The CSV is interpreted as a matrix, where the row marks the origin of an edge and the column marks the destination. Thus, loops are specified on the diagonal, while an asymmetric matrix creates different edge values for opposite directions. For an undirected graph, the matrix is automatically treated as symmetric. Trailing empty lines may be removed.

In the following example, the edges $a: b$ and $a: c$ are symmetric and there are no edges or self-loops $a: a$ or $b: b$. In contrast, $b: c$ is 3 whereas $c: b$ is 4 , and there is a self-loop $c: c$. The node $d$ only has an ingoing edge $\mathrm{b}: \mathrm{d}$, but no outgoing edges:

| a | b | c | d |
| :--- | :--- | :--- | :--- |
| 0 | 2 | 1 | 0 |
| 2 | 0 | 3 | 2 |
| 1 | 4 | 1 | 0 |

If undirected evaluates to True, the upper right corner is mirrored to the lower left. Note that the diagonal must be provided. The following matrices give the same output if symmetric is True:

| a | b | c | a | b | c | a | b | c |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 2 | 1 | 0 | 2 | 1 | 0 | 2 | 1 |
| 2 | 0 | 3 |  | 0 | 3 | 5 | 0 | 3 |
| 1 | 4 | 1 |  |  | 1 | 7 |  | 1 |

Each value is evaluated and filtered by literal_type and valid_edge:
graphi.graph_io.csv.literal_type (literal) $\rightarrow$ object
Fields read from the csv are passed to literal_type directly as the sole argument. The return value is considered as final, and inserted into the graph without further conversions.
graphi.graph_io.csv.valid_edge (object) $\rightarrow$ bool
Similarly, valid_edge is called on the result of literal_type. The default is bool (), which should work for most data types.
The default for literal_type is capable of handling regular python literals, e.g. int, float and str. In combination with valid_edge, any literal of non-True values signifies a missing edge: None, False, 0 etc.

See All *args and $* *$ kwargs are passed on directly to csv. reader for extracting lines.
graphi.graph_io.csv.stripped_literal (literal)
evaluate literals, ignoring leading/trailing whitespace
This function is capable of handling all literals supported by ast.literal_eval(), even if they are surrounded by whitespace.

## graphi.operators package

## Submodules

graphi.operators.interface module
graphi.types package

## Subpackages

graphi.types.cython_graph package

## Submodules

graphi.types.cython_graph.plain_graph module

## Submodules

graphi.types.adjacency_graph module

```
class graphi.types.adjacency_graph.AdjacencyGraph(*args, **kwargs)
```

Bases: graphi.abc.Graph
Graph storing edge distances via adjacency lists

## Parameters

- source - adjacency information
- undirected - whether the graph enforces symmetry

This graph provides optimal performance for random, direct access to nodes and edges. As it stores individual nodes and edges, it is optimal in both space and time for sparse graphs.

However, ordering of nodes (), edges () and values () is arbitrary. The expected complexity for searches is the worst case of $\mathrm{O}(\operatorname{len}(\operatorname{nodes}())=\mathrm{n})$ and $\mathrm{O}\left(\operatorname{len}(\operatorname{edges}())->\mathrm{n}^{2}\right)$, respectively.

## clear()

Remove all elements from this graph
edges ()
Return a new view of the graph's edges
Returns view of the graph's edges
Return type EdgeView
update (other)
Update the graph with the nodes, edges and values from other, overwriting existing elements.
Parameters other (Graph or ItemView) - graph or items from which to pull elements
values()
Return a new view of the values of the graph's edges
Returns view of the values of the graph's edges
Return type ValueView

```
class graphi.types.adjacency_graph.EdgeView (graph)
```

Bases: graphi.abc.EdgeView
View on the edges in a graph

```
class graphi.types.adjacency_graph.ValueView(graph)
```

Bases: graphi.abc.ValueView
View on the values of edges in a graph

## graphi.types.bounded module

class graphi.types.bounded.Bounded (*source, **kwargs)
Bases: graphi.abc.Graph
Wrapper to make the values of Graph instances bounded
Parameters value_bound - bound for all values
The value_bound must be compatible with all values stored in the graph. A TypeError is raised whenever a value cannot be bounded. Note that None is always invalid for value_bound.

## See also:

The boundable () decorator for Graph classes.

## clear()

Remove all elements from this graph
undirected
update (other)
Update the graph with the nodes, edges and values from other, overwriting existing elements.
Parameters other (Graph or ItemView) - graph or items from which to pull elements

## graphi.types.decorator module

```
graphi.types.decorator.boundable(graph_class)
```

Make an implementation of Graph bounded when passing value_bound to it

```
@boundable
class SomeGraph(abc.Graph):
unbounded_graph = SomeGraph()
bounded_graph = SomeGraph(value_bound=42)
```

This provides an implementation agnostic interface to ensure all edge values are bounded. For any nodes a and b , graph [a:b] <= value_bound always holds. Setting an edge value larger than value_bound removes the edge.
graphi.types.decorator.undirectable (graph_class)
Make an implementation of Graph undirected when passing undirected=True to it

```
@undirectable
class SomeGraph(abc.Graph):
```

directed_graph = SomeGraph()
undirected_graph $=$ SomeGraph(undirected=True)
This provides an implementation agnostic interface to ensure all edges are undirected. For any nodes a and b , graph [a:b] == graph[b:a] always holds and graph.edges () produces only one of $a: b$ or $b: a$.

## graphi.types.distance_graph module

class graphi.types.distance_graph.CachedDistanceGraph(*source, **kwargs)
Bases: graphi.types.distance_graph.DistanceGraph
Graph of nodes connected by a cached distance function
Compared to DistanceGraph, each edge is computed only once and stored for future lookup. Edges can be "deleted", which sets their value to an infinite value.

## Parameters

- nodes - all nodes contained in the graph
- distance - a function $\operatorname{dist}(a, b)$->object that computes the distance between any two nodes
- undirected - whether distance can be treated as undirected, i.e. $\operatorname{dist}(a, b)==\operatorname{dist}(b, a)$

Warning For N nodes, all NxN edges are exposed and stored. This may lead to O ( N :sup:2) runtime and memory complexity.
clear()
Remove all elements from this graph
class graphi.types.distance_graph.DistanceGraph(*args, **kwargs)
Bases: graphi.abc. Graph
Graph of nodes connected by a distance function

## Parameters

- nodes - all nodes contained in the graph
- distance - a function $\operatorname{dist}(a, b)$->object that computes the distance between any two nodes
- undirected - whether distance can be treated as undirected, i.e. $\operatorname{dist}(a, b)==\operatorname{dist}(b, a)$

Warning For N nodes, all NxN edges are exposed. This may lead to $\mathrm{O}(\mathrm{N}:$ sup:2) runtime complexity.
clear()
Remove all elements from this graph
update (other)
Update the graph with the nodes, edges and values from other, overwriting existing elements.
Parameters other (Graph or ItemView) - graph or items from which to pull elements

## graphi.types.undirected module

class graphi.types.undirected.Undirected(*source, **kwargs)
Bases: graphi.abc.Graph

Wrapper to make Graph instances undirected

## See also:

The undirectable () decorator for Graph classes.
clear ()
Remove all elements from this graph
edges ()
Return a new view of the graph's edges
Returns view of the graph's edges
Return type UndirectedEdgeView
undirected
update (other)
Update the graph with the nodes, edges and values from other, overwriting existing elements.
Parameters other (Graph or ItemView) - graph or items from which to pull elements
values()
Return a new view of the values of the graph's edges
Returns view of the values of the graph's edges
Return type UndirectedValueView
class graphi.types.undirected. UndirectedEdge (start, stop, step=None)
Bases: graphi.edge.Edge
An undirected edge as a pair of nodes
For any nodes a and b , the UndirectedEdges $\mathrm{a}: \mathrm{b}$ and $\mathrm{b}: \mathrm{a}$ are equivalent. As a result, which of the two is start or stop is arbitrary but well-defined.

```
class graphi.types.undirected.UndirectedEdgeView (graph)
```

Bases: graphi.abc.EdgeView
View on the undirected edges in a graph

```
class graphi.types.undirected.UndirectedValueView(graph)
```

Bases: graphi.abc.ValueView
View on the values of undirected edges in a graph

### 6.1.3 Submodules

graphi.abc module
class graphi.abc.AdjacencyList
Bases: dict, _abcoll.MutableMapping
Edge values of nodes to a node in a graph
This represents edges in a graph originating from node as a mapping to their values. For example, the edge graph [a:b] = c corresponds to adjacency [b] = c for node $a$.
exception graphi.abc.AdjacencyListTypeError (item)
Bases: exceptions.TypeError
AdjacencyList set with an incorrect type
class graphi.abc.AdjacencyView (graph, node)
Bases: graphi.abc.GraphView
View on the adjacency of edges for a node in a graph
This represents edges in a graph originating from node as a mapping-like view. For example, the edge graph [a:b] = c corresponds to adjacency [b] $=c$ for node $a$.
exception graphi.abc.EdgeError (edge)
Bases: exceptions.Exception
Graph edge not found
class graphi.abc.EdgeView (graph)
Bases: graphi.abc.GraphView
View on the edges in a graph
class graphi.abc.Graph (*source, **kwargs)
Bases: _abcoll. Container
Abstract Base Class for graphs representing values of edges between nodes
A Graph is a container for primitive nodes and edges. There are three types of elements handled by a graph:

1. primitive nodes,
2. slice-like edges as pairs of nodes, and
3. primitive edge values.

Both nodes and edge values are conceptually similar to keys and values of dict. However, the concept of node pairs as edges adds additional functionality. The fixed relation between arbitrary nodes $a, b$ and the directed pair $a$ : b creates two value-type layers:

1. each node is mapped to all its outgoing edges,
2. each edge is mapped to the respective edge value.

In short, graph [a] provides a collection of edges originating at $a$, while graph [a:b] provides the specific edge value from a to $b$.

Note: Many interfaces return the rich Edge type for its added usability. To access an edge value, using slice such as graph [a:b] is sufficient, however.

Similar to Mappings, nodes are the primary keys of a Graph. As a result, the container interfaces, such as iter and len, operate on nodes. In general, nodes can be of arbitrary type as long as they are hashable.
By default, edges in a Graph are directed and unique: The edges represented by graph[a:b] and graph [b:a] are separate with opposite direction. Each edge is unique, i.e. there is only one edge graph [a:b]. A loop is represented by the edge graph [a:a]. The edge entities stored in the graph may be arbitrary objects.

As such, the interface of Graph defaults to describing a directed graph. However, other types of graph can be expressed as well. These generally do not form separate types in term of implementation.

Multigraphs allow for multiple edges between pairs of nodes. In this case, all edge values are containers (such as list or set) of arbitrary size. Whether a Graph is a graph of containers or a multigraph depends on the context.

Undirected Graphs do not distinguish between graph [a:b] and graph [b:a]. This can be enforced by symmetry of edge values, which guarantees that graph $[\mathrm{a}: \mathrm{b}]==$ graph [b:a] always applies.

## g.undirected

Indicates whether Graph $g$ is guaranteed to be undirected, having only symmetric edge values. If True, $g[a: b]$ is $g[b: a]$ for any nodes $a$ and $b$ in $g$; the graph enforces this, e.g. $g[a: b]=c$ implies $g[b: a]=c$. If False, symmetric edges are allowed but not enforced.
Read-only unless explicitly indicated otherwise.
There are several ways to initialise a new graph; their main difference is which element types are left empty.

## Graph ()

Create a new empty graph. No nodes, edges or values are filled in.

## Graph (graph)

Create a new graph with all nodes, edges and values of graph. The resulting graph is a shallow copy of graph - the identity of elements is preserved.
Graph (a, b, c, ...)
Graph ([a, b, c, ...])
Graph (\{a, b, c, ...\})
Graph (<iterable for $a, b, c, \ldots$ )
Create a new graph with nodes $a, b, c, d$, and so on. No edges or values are created explicitly.

Graph(\{a: AdjacencyList(\{b: ab_edge, c: ...\}), b: AdjacencyList (...), ...\})
Create a new graph with nodes $a, b, c$, and so on. Initialize edges to graph [a:b] = ab_edge, graph[b:a] = ba_edge, and so on.

Note: If only a single argument is provided, graph and mapping initialization is preferred over iterable initialisation. To initialize a graph with a graph or mapping as the sole node, wrap it in an iterable, e.g. Graph ([graph]).

All implementations of this ABC guarantee the following operators:

## bool (g)

Whether there are any nodes in the graph $g$.

## len (g)

Return the number of nodes in the graph $g$.
g[a:b]
Return the value of the edge between nodes a and b. Raises EdgeError if no edge is defined for the nodes. Undirected graphs guarantee $g[a: b]==g[b: a]$.
$g[a: b]=$ value
Set the value of the edge between nodes $a$ and $b$ to value for graph $g$.
del $g[a: b]$
Remove the edge and value between nodes a and b from g . Raises EdgeError if the edge is not in the graph.
g[a]
Return the edges between nodes a and any other node as an AdjacencyList corresponding to $\{b$ : ab_edge, c: ac_edge, ...\}. Raises NodeError if a is not in $g$.
$g[a]=$ True
g.add (a)

Add the node a to graph $g$ if it does not exist. Do not add, remove or modify existing edges. Graphs for which edges are computed, not set, may create them implicitly.

Changed in version 0.3.0: Added g[a] = True, deprecated g[a] = andg[a] = None.

```
g[a] = {}
g[a] = AdjacencyList()
```

Add the node a to graph $g$ if it does not exist. Remove any existing edges originating at a from graph $g$.

```
g[a] = {b: ab_edge, c: ac_edge, ...}
g[a] = AdjacencyList (b=ab_edge, c=c_edge)
```

Add the node $a$ to graph $g$ if it does not exist. Set the value of the edge between nodes $a$ and $b$ to ab_edge, between a and c to ac_edge, and so on. Remove any other edge from a. Raises NodeError if any of $b, c$, etc. are not in $g$.

```
del g[a]
```

Remove the node a and all its edges from $g$. Raises NodeError if the node is not in the graph.
a in $g$
Return True if $g$ has a node $a$, else False.

```
Edge[a:b] in g
```

Edge (a, b) in $g$

Return True if $g$ has an edge from node $a$ to $b$, else False.

## iter (g)

Return an iterator over the nodes in $g$.
In addition, several methods are provided. While methods and operators for retrieving data must be implemented by all subclasses, methods for modifying data may not be applicable to certain graphs.

## add (item)

Safely add a node or edge to the graph, without modifying existing edges
If a node is not part of the graph, it is added without any explicit edges. If a edge is not part of the graph, its value is set to True.

Note: Graphs which compute edges may implicitly create new edges if node is new to the graph.
clear()
Remove all elements from this graph
copy ()
Return a shallow copy of this graph

## discard (item)

Remove a node or edge from the graph if it is a member
Parameters item - node or edge to discard from the graph
edges ()
Return a new view of the graph's edges
Returns view of the graph's edges
Return type EdgeView
get (item, default=None)
Return the value for node or edge item if it is in the graph, else default. If default is not given, it defaults to None, so that this method never raises a NodeError or EdgeError.

## Parameters

- item - node or edge to look up in the graph
- default - default to return if item is not in the graph


## items()

Return a new view of the graph's edges and their values
Returns view of the graph's edges and their values
Return type ItemView
nodes ()
Return a new view of the graph's nodes
Returns view of the graph's nodes
Return type NodeView
undirected = False
whether this graph is undirected, having only symmetric edges

## update (other)

Update the graph with the nodes, edges and values from other, overwriting existing elements.
Parameters other (Graph or ItemView) - graph or items from which to pull elements
values()
Return a new view of the values of the graph's edges
Returns view of the values of the graph's edges
Return type ValueView
class graphi.abc.GraphView (graph)
Bases: _abcoll.Sized
Dynamic view on the content of a Graph
View objects represent a portion of the content of a graph. A view allows to work with its scope without copying the viewed content. It is dynamic, meaning that any changes to the graph are reflected by the view.

Each view works only on its respective portion of the graph. For example, edge in nodeview will always return False.

## len (graphview)

Return the number of nodes, node pairs or edges in the graph.
$\mathbf{x}$ in graphview
Return True if x is a node, node pair or edge of the graph.

## iter (graphview)

Return an iterator over the nodes, node pairs or edges in the graph.
Each view strictly defines the use of nodes, edges or values. As such, edges are safely represented as a tuple of start and end node.
undirected

```
class graphi.abc.ItemView(graph)
```

Bases: graphi.abc.GraphView
View on the edges and values in a graph
Represents edges and their value as a tuple of (tail, head, value). For example, the edge graph $[a: b]=c$ corresponds to the item $(a, b, c)$.
exception graphi.abc.NodeError (node)
Bases: exceptions.Exception
Graph node not found
class graphi.abc.NodeView (graph)
Bases: graphi.abc. GraphView
View on the nodes of a graph
class graphi.abc.ValueView (graph)
Bases: graphi.abc.GraphView
View on the values of edges in a graph

## graphi.edge module

class graphi.edge.Edge (start, stop, step=None)
Bases: ob ject
An edge in a graph as a pair of nodes

## Parameters

- start - the start or tail of an edge
- stop - the stop or head of an edge
- step - currently unused

This is a verbose interface for creating edges between nodes for use in a graph. It allows using slice notation independent of a graph:

```
>>> atb = Edge[a:b]
>>> a2b = Edge(a, b)
>>> graph[a2b] = 1337
>>> graph[a:b] == graph[atb] == graph[a2b] == graph[Edge[a:b]] == graph[Edge(a,的
@b) ]
True
```

A Edge can also be used for explicit containment tests:

```
>>> Edge[a:b] in graph
True
```

In addition to their slice-like nature, Edge is iterable and indexable. This allows for easy unpacking:

```
>>> edge = Edge[a:b]
>>> tail, head = edge
```

Note: This class creates a representation of an edge as a connection between nodes. Edge values can be arbitrary objects.

Warning: Even though Edge behaves like a slice in graphs, builtin containers such as list cannot make use of an Edge.

```
start
stop
```

```
class graphi.edge.EdgeMeta
```

Bases: type
Metaclass for Edge to support Edge [a:b]
class graphi.edge.Loop (start, stop $=$ None, step $=$ None)
Bases: graphi.edge.Edge
An edge in a graph from a node to itself

## Parameters

- start - the start or tail of a loop
- stop - optional stop or head of a loop, same as start
- step - currently unused

Raises ValueError - if stop is given but not equal to start

$$
\underbrace{\text { flighttime }}_{\text {graph }}[\overbrace{\underbrace{\text { Berlin }}_{\text {node }}: \underbrace{\text { London }}_{\text {node }}}^{\text {edge }}]=\underbrace{3900}_{\text {value }}
$$

Graph I is a lightweight graph library - it is suitable to model networks, connections and other relationships. Compared to other graph libraries, GraphI aims for being as pythonic as possible. If you are comfortable using list, dict or other types, GraphI is intuitive and straight-forward to use.

```
# create a graph with initial nodes
from graphi import graph
airports = graph("New York", "Rio", "Tokyo")
# add connections between nodes
airports["New York":"Rio"] = timedelta(hours=9, minutes=50)
airports["New York":"Tokyo"] = timedelta(hours=13, minutes=55)
```

At its heart, Graph I is built to integrate with Python's data model. It natively works with primitives, iterables, mappings and whatever you need. For example, creating a multigraph is as simple as using multiple edge values:

```
# add multiple connections between nodes -> Multigraph
airports["Rio":"Tokyo"] = timedelta(days=1, hours=2), timedelta(days=1, hours=3)
```

By design, Graph I is primarily optimized for general convenience over specific brute force performance. It heavily exploits lazy iteration, data views and other modern python paradigms under the hood. This allows the use of common operations without loss of performance:

```
# get number of outgoing edges of nodes -> outdegree
outgoing_flights = {city: len(airports[city]) for city in airports}
```

With its general-purpose design, Graph I makes no assumptions about your data. You are free to use whatever is needed to solve your problem.

## CHAPTER 7

## Frequently Asked Questions

Yet another graph library? The goal of Graph I is not to be another graph library, but to provide an intuitive way to work with graphs. Working with complex graphs should be as easy for you as working with any other primitive type.

Graph I is suitable for interactive, explorative use. At the same time, it also allows for a seamless specialisation to optimised data structures.

What parts do I actually need? The GraphI library provides several points of interest:

- The graphi.graph type, the most performant general purpose graph type available. Use this as the starting point, the way you would use dict, list and others.
- The graphi.types module which offers various graph types for different use-cases. Use this for specialisation, the way you would use numpy . array and others.
- The graphi.types.decorator helpers which can produce undirected and bounded graph types. Use this for custom types to quickly provide variants from directed graphs.
- The graphi. abc which allows to code against several different graph implementations. Use this for generic algorithms, the way you would use collections.abc types.

What is this thing you call $\boldsymbol{A B C}$ ? Graph I does not just provide graph implementations, but also an efficient graph interface. This interface is defined by the graphi.abc abstract base classes.

Any custom graph implementation can be made a virtual subclass of these ABCs. This allows you to adopt graph implementations optimized for your use-case without changing your code.
Where are all the algorithms? First and foremost, GraphI is designed for you to work on graph data instead of pre-sliced storybook data. GraphI implements only algorithms that

1. are fundamental building blocks for advanced algorithms, and/or
2. benefit from knowledge of internal data structures.

At the moment, you can find basic operators in the graphi.operators module.
What about performance? At its core, GraphI uses Python's native, highly optimized data structures. For any nontrivial graph algorithm, the provided performance is more than sufficient.

From our experience, performance critical code is best run with PyPy. This will not just optimize isolated pieces, but the actual combination of your algorithm and GraphI as a whole.
For CPython, an optimised graph type implemented in C is available. Note that graphi.graph will always represent the most optimised graph type available.

- genindex
- modindex
- search

Documentation built from graphi 0.3.0 at Nov 16, 2018.

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